

COTS Embedded Database Solving Dynamic Points-of- Interest

Abstract

In navigation devices of today the This article looks at how commercial off the shelf (COTS) database solutions can be utilized to solve the dynamic point of interest problem.

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1 INTRODUCTION

Navigation systems found in cars and handheld units provide an efficient and easy way to lookup points of interest in a city, find the best route to a user's destination and provide other regionally-based operations by efficiently managing map points. A typical query for these devices is for example locating the nearest Italian restaurant based on the current position of the vehicle. Proprietary data sets and indexing algorithms are used to solve these types of queries, but a major drawback with most of these devices is that they are 'read only' to prevent users from making changes and corrupting the dataset. Updates to datasets must be done in batch mode, and the complete dataset and indexes must be rebuilt on a regular basis because new businesses are constantly cropping up and new roads and buildings are being constructed. Vendors are therefore unable to offer customers localized datasets which could be sold at gas stations and other venues, nor can users make route calculations on the fly to avoid ad-hoc obstacles like accidents.

2 COMMERCIAL OFF THE SHELF (COTS) SOLUTION

COTS embedded databases are designed to manage changing datasets and indexes without the chance of data corruption, but they have a different problem - they don't support two dimensional indexes needed to efficiently manage points-of-interest. If we can find a solution where COTS engines could be used, navigation vendors would be able to design more robust devices and provide new services to their customers.

The problem stems from the fact that a point of interest must be indexed based on both its longitude and latitude value where neither of the two values is favored. By default a one dimensional index will favor one of the two values making a range query very inefficient, which is the main reason why vendors create their own proprietary solutions.

| | | Longitude Values | | | | | | | | | | | | | | | |
|-----------------|----|------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|---------|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Latitude Values | 0 | (0,0) | (1,0) | (2,0) | (3,0) | (4,0) | (5,0) | (6,0) | (7,0) | (8,0) | (9,0) | (10,0) | (11,0) | (12,0) | (13,0) | (14,0) | (15,0) |
| | 1 | (0,1) | (1,1) | (2,1) | (3,1) | (4,1) | (5,1) | (6,1) | (7,1) | (8,1) | (9,1) | (10,1) | (11,1) | (12,1) | (13,1) | (14,1) | (15,1) |
| | 2 | (0,2) | (1,2) | (2,2) | (3,2) | (4,2) | (5,2) | (6,2) | (7,2) | (8,2) | (9,2) | (10,2) | (11,2) | (12,2) | (13,2) | (14,2) | (15,2) |
| | 3 | (0,3) | (1,3) | (2,3) | (3,3) | (4,3) | (5,3) | (6,3) | (7,3) | (8,3) | (9,3) | (10,3) | (11,3) | (12,3) | (13,3) | (14,3) | (15,3) |
| | 4 | (0,4) | (1,4) | (2,4) | (3,4) | (4,4) | (5,4) | (6,4) | (7,4) | (8,4) | (9,4) | (10,4) | (11,4) | (12,4) | (13,4) | (14,4) | (15,4) |
| | 5 | (0,5) | (1,5) | (2,5) | (3,5) | (4,5) | (5,5) | (6,5) | (7,5) | (8,5) | (9,5) | (10,5) | (11,5) | (12,5) | (13,5) | (14,5) | (15,5) |
| | 6 | (0,6) | (1,6) | (2,6) | (3,6) | (4,6) | (5,6) | (6,6) | (7,6) | (8,6) | (9,6) | (10,6) | (11,6) | (12,6) | (13,6) | (14,6) | (15,6) |
| | 7 | (0,7) | (1,7) | (2,7) | (3,7) | (4,7) | (5,7) | (6,7) | (7,7) | (8,7) | (9,7) | (10,7) | (11,7) | (12,7) | (13,7) | (14,7) | (15,7) |
| | 8 | (0,8) | (1,8) | (2,8) | (3,8) | (4,8) | (5,8) | (6,8) | (7,8) | (8,8) | (9,8) | (10,8) | (11,8) | (12,8) | (13,8) | (14,8) | (15,8) |
| | 9 | (0,9) | (1,9) | (2,9) | (3,9) | (4,9) | (5,9) | (6,9) | (7,9) | (8,9) | (9,9) | (10,9) | (11,9) | (12,9) | (13,9) | (14,9) | (15,9) |
| | 10 | (0,10) | (1,10) | (2,10) | (3,10) | (4,10) | (5,10) | (6,10) | (7,10) | (8,10) | (9,10) | (10,10) | (11,10) | (12,10) | (13,10) | (14,10) | (15,10) |
| | 11 | (0,11) | (1,11) | (2,11) | (3,11) | (4,11) | (5,11) | (6,11) | (7,11) | (8,11) | (9,11) | (10,11) | (11,11) | (12,11) | (13,11) | (14,11) | (15,11) |
| | 12 | (0,12) | (1,12) | (2,12) | (3,12) | (4,12) | (5,12) | (6,12) | (7,12) | (8,12) | (9,12) | (10,12) | (11,12) | (12,12) | (13,12) | (14,12) | (15,12) |
| | 13 | (0,13) | (1,13) | (2,13) | (3,13) | (4,13) | (5,13) | (6,13) | (7,13) | (8,13) | (9,13) | (10,13) | (11,13) | (12,13) | (13,13) | (14,13) | (15,13) |
| | 14 | (0,14) | (1,14) | (2,14) | (3,14) | (4,14) | (5,14) | (6,14) | (7,14) | (8,14) | (9,14) | (10,14) | (11,14) | (12,14) | (13,14) | (14,14) | (15,14) |
| | 15 | (0,15) | (1,15) | (2,15) | (3,15) | (4,15) | (5,15) | (6,15) | (7,15) | (8,15) | (9,15) | (10,15) | (11,15) | (12,15) | (13,15) | (14,15) | (15,15) |

Figure 1

Figure 1 is a longitude, latitude grid of all points in a system where both the longitude and latitude are coded as 4 bit values. In real world applications these values would be 32 bit but for the simplicity of describing both the problem and solution, the maps in this article will be based on 4 bit data types.

A one dimensional index, such as a B-Tree, will only provide an efficient longitude/latitude index in one direction. In the figure, the longitude values are illustrated as the most significant information so the index will only have vertical efficiency. Think of the value in each cell as what the index sees, and the index is sorted from low to high.

If we add a region query based on the bounding box between (5, 5) to (9, 8) this would translate to a range scan of the index between the two values. Figure 2 illustrates exactly that.

| | | Longitude Values | | | | | | | | | | | | | | | |
|-----------------|----|------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|---------|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Latitude Values | 0 | (0,0) | (1,0) | (2,0) | (3,0) | (4,0) | (5,0) | (6,0) | (7,0) | (8,0) | (9,0) | (10,0) | (11,0) | (12,0) | (13,0) | (14,0) | (15,0) |
| | 1 | (0,1) | (1,1) | (2,1) | (3,1) | (4,1) | (5,1) | (6,1) | (7,1) | (8,1) | (9,1) | (10,1) | (11,1) | (12,1) | (13,1) | (14,1) | (15,1) |
| | 2 | (0,2) | (1,2) | (2,2) | (3,2) | (4,2) | (5,2) | (6,2) | (7,2) | (8,2) | (9,2) | (10,2) | (11,2) | (12,2) | (13,2) | (14,2) | (15,2) |
| | 3 | (0,3) | (1,3) | (2,3) | (3,3) | (4,3) | (5,3) | (6,3) | (7,3) | (8,3) | (9,3) | (10,3) | (11,3) | (12,3) | (13,3) | (14,3) | (15,3) |
| | 4 | (0,4) | (1,4) | (2,4) | (3,4) | (4,4) | (5,4) | (6,4) | (7,4) | (8,4) | (9,4) | (10,4) | (11,4) | (12,4) | (13,4) | (14,4) | (15,4) |
| | 5 | (0,5) | (1,5) | (2,5) | (3,5) | (4,5) | (5,5) | (6,5) | (7,5) | (8,5) | (9,5) | (10,5) | (11,5) | (12,5) | (13,5) | (14,5) | (15,5) |
| | 6 | (0,6) | (1,6) | (2,6) | (3,6) | (4,6) | (5,6) | (6,6) | (7,6) | (8,6) | (9,6) | (10,6) | (11,6) | (12,6) | (13,6) | (14,6) | (15,6) |
| | 7 | (0,7) | (1,7) | (2,7) | (3,7) | (4,7) | (5,7) | (6,7) | (7,7) | (8,7) | (9,7) | (10,7) | (11,7) | (12,7) | (13,7) | (14,7) | (15,7) |
| | 8 | (0,8) | (1,8) | (2,8) | (3,8) | (4,8) | (5,8) | (6,8) | (7,8) | (8,8) | (9,8) | (10,8) | (11,8) | (12,8) | (13,8) | (14,8) | (15,8) |
| | 9 | (0,9) | (1,9) | (2,9) | (3,9) | (4,9) | (5,9) | (6,9) | (7,9) | (8,9) | (9,9) | (10,9) | (11,9) | (12,9) | (13,9) | (14,9) | (15,9) |
| | 10 | (0,10) | (1,10) | (2,10) | (3,10) | (4,10) | (5,10) | (6,10) | (7,10) | (8,10) | (9,10) | (10,10) | (11,10) | (12,10) | (13,10) | (14,10) | (15,10) |
| | 11 | (0,11) | (1,11) | (2,11) | (3,11) | (4,11) | (5,11) | (6,11) | (7,11) | (8,11) | (9,11) | (10,11) | (11,11) | (12,11) | (13,11) | (14,11) | (15,11) |
| | 12 | (0,12) | (1,12) | (2,12) | (3,12) | (4,12) | (5,12) | (6,12) | (7,12) | (8,12) | (9,12) | (10,12) | (11,12) | (12,12) | (13,12) | (14,12) | (15,12) |
| | 13 | (0,13) | (1,13) | (2,13) | (3,13) | (4,13) | (5,13) | (6,13) | (7,13) | (8,13) | (9,13) | (10,13) | (11,13) | (12,13) | (13,13) | (14,13) | (15,13) |
| | 14 | (0,14) | (1,14) | (2,14) | (3,14) | (4,14) | (5,14) | (6,14) | (7,14) | (8,14) | (9,14) | (10,14) | (11,14) | (12,14) | (13,14) | (14,14) | (15,14) |
| | 15 | (0,15) | (1,15) | (2,15) | (3,15) | (4,15) | (5,15) | (6,15) | (7,15) | (8,15) | (9,15) | (10,15) | (11,15) | (12,15) | (13,15) | (14,15) | (15,15) |

Figure 2

Not only are the yellow points returned to the application but also all the false gray points that are clearly outside the bounding box. This inefficiency is the major reason for navigational vendors implementing proprietary solutions based on two dimensional indexing algorithms like R-Tree or any of its cousins. By making the proprietary implementation read only, the vendors don't need to implement transactional safety or concurrency control to avoid corruption or allow multi-threaded application access to the data.

3 IMPLEMENTATION

This article will describe a solution to the two dimensional problem by mapping it down to one dimension allowing us to leverage all the investments done in the embedded database space. This not only allows the vendors to efficiently query these points-of-interest but also allows them to dynamically add other one dimensional information to the query, like type (gas station, restaurant, etc), which can't be solved with a two dimensional index system.

If you look at the previous figure, the one dimensional index is inefficient since its most significant piece of information is taken from the Longitude values and the second most significant from the latitude, thus creating the undesired vertical efficiency. If you translate the points into the bit pattern used by the indexing system it will look like this:

| | | Longitude Values | | | | | | | | | | | | | | | |
|-----------------|----|------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Latitude Values | 0 | 00000000 | 00010000 | 00100000 | 00110000 | 01000000 | 01010000 | 01100000 | 01110000 | 10000000 | 10010000 | 10100000 | 10110000 | 11000000 | 11010000 | 11100000 | 11110000 |
| | 1 | 00000001 | 00010001 | 00100001 | 00110001 | 01000001 | 01010001 | 01100001 | 01110001 | 10000001 | 10010001 | 10100001 | 10110001 | 11000001 | 11010001 | 11100001 | 11110001 |
| | 2 | 00000010 | 00010010 | 00100010 | 00110010 | 01000010 | 01010010 | 01100010 | 01110010 | 10000010 | 10010010 | 10100010 | 10110010 | 11000010 | 11010010 | 11100010 | 11110010 |
| | 3 | 00000011 | 00010011 | 00100011 | 00110011 | 01000011 | 01010011 | 01100011 | 01110011 | 10000011 | 10010011 | 10100011 | 10110011 | 11000011 | 11010011 | 11100011 | 11110011 |
| | 4 | 00000100 | 00010100 | 00100100 | 00110100 | 01000100 | 01010100 | 01100100 | 01110100 | 10000100 | 10010100 | 10100100 | 10110100 | 11000100 | 11010100 | 11100100 | 11110100 |
| | 5 | 00000101 | 00010101 | 00100101 | 00110101 | 01000101 | 01010101 | 01100101 | 01110101 | 10000101 | 10010101 | 10100101 | 10110101 | 11000101 | 11010101 | 11100101 | 11110101 |
| | 6 | 00000110 | 00010110 | 00100110 | 00110110 | 01000110 | 01010110 | 01100110 | 01110110 | 10000110 | 10010110 | 10100110 | 10110110 | 11000110 | 11010110 | 11100110 | 11110110 |
| | 7 | 00000111 | 00010111 | 00100111 | 00110111 | 01000111 | 01010111 | 01100111 | 01110111 | 10000111 | 10010111 | 10100111 | 10110111 | 11000111 | 11010111 | 11100111 | 11110111 |
| | 8 | 00001000 | 00011000 | 00101000 | 00111000 | 01001000 | 01011000 | 01101000 | 01111000 | 10001000 | 10011000 | 10101000 | 10111000 | 11001000 | 11011000 | 11101000 | 11111000 |
| | 9 | 00001001 | 00011001 | 00101001 | 00111001 | 01001001 | 01011001 | 01101001 | 01111001 | 10001001 | 10011001 | 10101001 | 10111001 | 11001001 | 11011001 | 11101001 | 11111001 |
| | 10 | 00001010 | 00011010 | 00101010 | 00111010 | 01001010 | 01011010 | 01101010 | 01111010 | 10001010 | 10011010 | 10101010 | 10111010 | 11001010 | 11011010 | 11101010 | 11111010 |
| | 11 | 00001011 | 00011011 | 00101011 | 00111011 | 01001011 | 01011011 | 01101011 | 01111011 | 10001011 | 10011011 | 10101011 | 10111011 | 11001011 | 11011011 | 11101011 | 11111011 |
| | 12 | 00001100 | 00011100 | 00101100 | 00111100 | 01001100 | 01011100 | 01101100 | 01111100 | 10001100 | 10011100 | 10101100 | 10111100 | 11001100 | 11011100 | 11101100 | 11111100 |
| | 13 | 00001101 | 00011101 | 00101101 | 00111101 | 01001101 | 01011101 | 01101101 | 01111101 | 10001101 | 10011101 | 10101101 | 10111101 | 11001101 | 11011101 | 11101101 | 11111101 |
| | 14 | 00001110 | 00011110 | 00101110 | 00111110 | 01001110 | 01011110 | 01101110 | 01111110 | 10001110 | 10011110 | 10101110 | 10111110 | 11001110 | 11011110 | 11101110 | 11111110 |
| | 15 | 00001111 | 00011111 | 00101111 | 00111111 | 01001111 | 01011111 | 01101111 | 01111111 | 10001111 | 10011111 | 10101111 | 10111111 | 11001111 | 11011111 | 11101111 | 11111111 |

Figure 3

The four most significant bits ($x_4x_3x_2x_1$) stem from the Longitude value and the 4 second most significant bits ($y_4y_3y_2y_1$) stem from the Latitude. Let's introduce the Z-value¹, which is made up of interleaving the most significant bits from both dimensions, resulting in values on the form ($y_4x_4y_3x_3y_2x_2y_1x_1$). If our one dimensional index uses this bit pattern as its index values we'll be indexing something where the most significant information from both dimensions is taken into consideration. Figure 4 shows the pattern.

¹ Morton, G. M. (1966), A computer Oriented Geodetic Data Base; and a New Technique in File Sequencing, Technical Report, Ottawa, Canada: IBM Ltd.

| | | Longitude Values | | | | | | | | | | | | | | | |
|-----------------|----|------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Latitude Values | 0 | 00000000 0 | 00000001 1 | 00000100 4 | 00000101 5 | 00010000 16 | 00010001 17 | 00010100 20 | 00010101 21 | 01000000 64 | 01000001 65 | 01000100 68 | 01000101 69 | 01010000 80 | 01010001 81 | 01010100 84 | 01010101 85 |
| | 1 | 00000010 2 | 00000011 3 | 00000110 6 | 00000111 7 | 00010010 18 | 00010011 19 | 00010110 22 | 00010111 23 | 01000010 66 | 01000011 67 | 01000110 70 | 01000111 71 | 01010010 82 | 01010011 83 | 01010110 86 | 01010111 87 |
| | 2 | 00001000 8 | 00001001 9 | 00001100 12 | 00001101 13 | 00011000 24 | 00011001 25 | 00011100 28 | 00011101 29 | 01001000 72 | 01001001 73 | 01001100 76 | 01001101 77 | 01011000 88 | 01011001 89 | 01011100 92 | 01011101 93 |
| | 3 | 00001010 10 | 00001011 11 | 00001110 14 | 00001111 15 | 00011010 26 | 00011011 27 | 00011110 30 | 00011111 31 | 01001010 74 | 01001011 75 | 01001110 78 | 01001111 79 | 01011010 90 | 01011011 91 | 01011110 94 | 01011111 95 |
| | 4 | 00100000 32 | 00100001 33 | 00100100 36 | 00100101 37 | 00110000 48 | 00110001 49 | 00110100 52 | 00110101 53 | 01100000 96 | 01100001 97 | 01100100 100 | 01100101 101 | 01110000 112 | 01110001 113 | 01110100 116 | 01110101 117 |
| | 5 | 00100010 34 | 00100011 35 | 00100110 38 | 00100111 39 | 00110010 50 | 00110011 51 | 00110110 54 | 00110111 55 | 01100010 98 | 01100011 99 | 01100110 102 | 01100111 103 | 01110010 114 | 01110011 115 | 01110110 118 | 01110111 119 |
| | 6 | 00101000 40 | 00101001 41 | 00101100 44 | 00101101 45 | 00111000 56 | 00111001 57 | 00111100 60 | 00111101 61 | 01101000 104 | 01101001 105 | 01101100 108 | 01101101 109 | 01111000 120 | 01111001 121 | 01111100 124 | 01111101 125 |
| | 7 | 00101010 42 | 00101011 43 | 00101110 46 | 00101111 47 | 00111010 58 | 00111011 59 | 00111110 62 | 00111111 63 | 01101010 106 | 01101011 107 | 01101110 110 | 01101111 111 | 01111010 122 | 01111011 123 | 01111110 126 | 01111111 127 |
| | 8 | 10000000 128 | 10000001 129 | 10000100 132 | 10000101 133 | 10010000 144 | 10010001 145 | 10010100 148 | 10010101 149 | 11000000 192 | 11000001 193 | 11000100 196 | 11000101 197 | 11010000 208 | 11010001 209 | 11010100 212 | 11010101 213 |
| | 9 | 10000010 130 | 10000011 131 | 10000110 134 | 10000111 135 | 10010010 146 | 10010011 147 | 10010110 150 | 10010111 151 | 11000010 194 | 11000011 195 | 11000110 198 | 11000111 199 | 11010010 210 | 11010011 211 | 11010110 214 | 11010111 215 |
| | 10 | 10001000 136 | 10001001 137 | 10001100 140 | 10001101 141 | 10011000 152 | 10011001 153 | 10011100 156 | 10011101 157 | 11001000 200 | 11001001 201 | 11001100 204 | 11001101 205 | 11011000 216 | 11011001 217 | 11011100 220 | 11011101 221 |
| | 11 | 10001010 138 | 10001011 139 | 10001110 142 | 10001111 143 | 10011010 154 | 10011011 155 | 10011110 158 | 10011111 159 | 11001010 202 | 11001011 203 | 11001110 206 | 11001111 207 | 11011010 218 | 11011011 219 | 11011110 222 | 11011111 223 |
| | 12 | 10100000 160 | 10100001 161 | 10100100 164 | 10100101 165 | 10110000 176 | 10110001 177 | 10110100 180 | 10110101 181 | 11100000 224 | 11100001 225 | 11100100 228 | 11100101 229 | 11110000 240 | 11110001 241 | 11110100 244 | 11110101 245 |
| | 13 | 10100010 162 | 10100011 163 | 10100110 166 | 10100111 167 | 10110010 178 | 10110011 179 | 10110110 182 | 10110111 183 | 11100010 226 | 11100011 227 | 11100110 230 | 11100111 231 | 11110010 242 | 11110011 243 | 11110110 246 | 11110111 247 |
| | 14 | 10101000 168 | 10101001 169 | 10101100 172 | 10101101 173 | 10111000 184 | 10111001 185 | 10111100 188 | 10111101 189 | 11101000 232 | 11101001 233 | 11101100 236 | 11101101 237 | 11111000 248 | 11111001 249 | 11111100 252 | 11111101 253 |
| | 15 | 10101010 170 | 10101011 171 | 10101110 174 | 10101111 175 | 10111010 186 | 10111011 187 | 10111110 190 | 10111111 191 | 11101010 234 | 11101011 235 | 11101110 238 | 11101111 239 | 11111010 250 | 11111011 251 | 11111110 254 | 11111111 255 |

Figure 4

For illustration purposes each cell has both the binary and decimal representation of the Z-Values. Instead of having vertical efficiency we've now managed to introduce square like efficiency, but we still can't take any random region and expect an efficient result. If our bounding box happened to be from (0, 0) to (3, 3) or (6, 6) to (7, 7) we'd be extremely efficient since any query will be mapped to a range query and all points in our region have contiguous increasing value. E.g. the (0, 0) to (3, 3) bounding box resulting in a range query from 0 to 15.

Let's look at the range query from (5, 5) to (9, 8) that we were initially working on, How would that look?

| | | Longitude Values | | | | | | | | | | | | | | | |
|-----------------|----|------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Latitude Values | 0 | 00000000 0 | 00000001 1 | 00000100 4 | 00000101 5 | 00010000 16 | 00010001 17 | 00010100 20 | 00010101 21 | 01000000 64 | 01000001 65 | 01000100 68 | 01000101 69 | 01010000 80 | 01010001 81 | 01010100 84 | 01010101 85 |
| | 1 | 00000010 2 | 00000011 3 | 00000110 6 | 00000111 7 | 00010010 18 | 00010011 19 | 00010110 22 | 00010111 23 | 01000010 66 | 01000011 67 | 01000110 70 | 01000111 71 | 01010010 82 | 01010011 83 | 01010110 86 | 01010111 87 |
| | 2 | 00001000 8 | 00001001 9 | 00001100 12 | 00001101 13 | 00010000 24 | 00010001 25 | 00010100 28 | 00010101 29 | 01001000 72 | 01001001 73 | 01001100 76 | 01001101 77 | 01010000 88 | 01010001 89 | 01010100 92 | 01010101 93 |
| | 3 | 00001010 10 | 00001011 11 | 00001110 14 | 00001111 15 | 00010010 26 | 00010011 27 | 00010110 30 | 00010111 31 | 01001010 74 | 01001011 75 | 01001110 78 | 01001111 79 | 01010010 90 | 01010011 91 | 01010110 94 | 01010111 95 |
| | 4 | 00100000 32 | 00100001 33 | 00100100 36 | 00100101 37 | 00110000 48 | 00110001 49 | 00110100 52 | 00110101 53 | 01100000 96 | 01100001 97 | 01100100 100 | 01100101 101 | 01110000 112 | 01110001 113 | 01110100 116 | 01110101 117 |
| | 5 | 00100010 34 | 00100011 35 | 00100110 38 | 00100111 39 | 00110010 50 | 00110011 51 | 00110110 54 | 00110111 55 | 01100010 98 | 01100011 99 | 01100110 102 | 01100111 103 | 01110010 114 | 01110011 115 | 01110110 118 | 01110111 119 |
| | 6 | 00101000 40 | 00101001 41 | 00101100 44 | 00101101 45 | 00111000 56 | 00111001 57 | 00111100 60 | 00111101 61 | 01101000 104 | 01101001 105 | 01101100 108 | 01101101 109 | 01110000 120 | 01110001 121 | 01110100 124 | 01110101 125 |
| | 7 | 00101010 42 | 00101011 43 | 00101110 46 | 00101111 47 | 00111010 58 | 00111011 59 | 00111110 62 | 00111111 63 | 01101010 106 | 01101011 107 | 01101110 110 | 01101111 111 | 01110010 122 | 01110011 123 | 01110110 126 | 01110111 127 |
| | 8 | 10000000 128 | 10000001 129 | 10000100 132 | 10000101 133 | 10010000 144 | 10010001 145 | 10010100 148 | 10010101 149 | 11000000 192 | 11000001 193 | 11000100 196 | 11000101 197 | 11010000 208 | 11010001 209 | 11010100 212 | 11010101 213 |
| | 9 | 10000010 130 | 10000011 131 | 10000110 134 | 10000111 135 | 10010010 146 | 10010011 147 | 10010110 150 | 10010111 151 | 11000010 194 | 11000011 195 | 11000110 198 | 11000111 199 | 11010010 210 | 11010011 211 | 11010110 214 | 11010111 215 |
| | 10 | 10001000 136 | 10001001 137 | 10001100 140 | 10001101 141 | 10010000 152 | 10010001 153 | 10010100 156 | 10010101 157 | 11001000 200 | 11001001 201 | 11001100 204 | 11001101 205 | 11010000 216 | 11010001 217 | 11010100 220 | 11010101 221 |
| | 11 | 10001010 138 | 10001011 139 | 10001110 142 | 10001111 143 | 10010100 154 | 10010101 155 | 10010110 158 | 10010111 159 | 11001010 202 | 11001011 203 | 11001110 206 | 11001111 207 | 11010010 218 | 11010011 219 | 11010110 222 | 11010111 223 |
| | 12 | 10100000 160 | 10100001 161 | 10100100 164 | 10100101 165 | 10110000 176 | 10110001 177 | 10110100 180 | 10110101 181 | 11100000 224 | 11100001 225 | 11100100 228 | 11100101 229 | 11110000 240 | 11110001 241 | 11110100 244 | 11110101 245 |
| | 13 | 10100010 162 | 10100011 163 | 10100110 166 | 10100111 167 | 10110010 178 | 10110011 179 | 10110110 182 | 10110111 183 | 11100010 226 | 11100011 227 | 11100110 230 | 11100111 231 | 11110010 242 | 11110011 243 | 11110110 246 | 11110111 247 |
| | 14 | 10101000 168 | 10101001 169 | 10101100 172 | 10101101 173 | 10110000 184 | 10110001 185 | 10110100 188 | 10110101 189 | 11101000 232 | 11101001 233 | 11101100 236 | 11101101 237 | 11110000 248 | 11110001 249 | 11110100 252 | 11110101 253 |
| | 15 | 10101010 170 | 10101011 171 | 10101110 174 | 10101111 175 | 10110010 186 | 10110011 187 | 10110110 190 | 10110111 191 | 11101010 234 | 11101011 235 | 11101110 238 | 11101111 239 | 11110010 250 | 11110011 251 | 11110110 254 | 11110111 255 |

Figure 5

A straight forward range query of this region would return a whole lot of false points, (the grey points), which make this just as inefficient as the previous discussion. So the question is, can we optimize our query? The answer is yes. Since our points are now organized in squares we can take the region and break it down into multiple squares of contiguous increasing index values. You'll see from the rest of this discussion that the proposed algorithm for calculating these squares will result in our yellow region being broken into 5 smaller squares, scanned separately, optimizing out most of the false points.

| | | | | |
|-----------------|-----------------|-----------------|-----------------|-----------------|
| 00110011 51 | 00110110 54 | 00110111 55 | 01100010 98 | 01100011 99 |
| 00111001 57 | 00111100 60 | 00111101 61 | 01101000 104 | 01101001 105 |
| 00111011 59 | 00111110 62 | 00111111 63 | 01101010 106 | 01101011 107 |
| 10010001 145 | 10010100 148 | 10010101 149 | 11000000 192 | 11000001 193 |

We'll start out by doing a range query from 51 to 193, which are our bounding box values. As we scan we'll decide to calculate a region division if 3 false points are reported. We allow up to 3 false points to avoid too many division calculations. In our case the first division calculation will take place when the last reported point is above 63 and lower than 98 given that there are more than 3 points to report in this interval.

To illustrate the division calculation we've broken out the bounding box values in binary form:

```
51 = 00110011 = (0101,0101), and
193 = 11000001 = (1001,1000)
```

The first thing we do is look at the Z value and determine the first significant bit that differs based on the values; this will determine whether we're looking at a vertical or a horizontal division. With the above numbers the identified bit is z_8 which translates to the y_4 bit. Y bits will result in a horizontal split, x bits vertical.

Since we've identified a vertical split we know that the upper x boundary can be inherited from the 193 value and the lower x boundary from the 51. The two points we want to identify in this division (we'll call them LitMax and BigMin) are 107 and 145 which are the highest number in the upper square and lowest number in the bottom square divided by the red line. What we don't know is the y value just above and below this division line. LitMax's y value can be calculated as 'all common most significant bits' from the bounding box y values followed by a 0 and then 1's, and the BigMin's y value would be 'all common most significant bits' followed by 1 and then 0's.

So in our case we take the y's from 51 and 193 and look at the bit patterns:

```
51's y = 0101
193's y = 1000
```

This gives us the LitMax y value to be 0111 (no common bits), and BigMin's y value 1000 resulting in the LitMax point being (1001,0111) and BigMin's point being (0101,1000) interleaved resulting in 01101011 = 107 and 10010001 = 145.

Now that the calculation is done, our initial bounding box (5,5) to (9,8) is split in two - (5,5) to (9,7) and (5,8) to (9,8) . Since our last reported point was between 63 and 98 (less than LitMax) there is a chance of finding more valid points in the first region so we do a recursive call into the division algorithm with the new bounding box values, 51 to 107.

```
51 = 00110011 = (0101,0101), and
107 = 01101011 = (1001,0111)
```

Identifying that x_4 is the first significant bit that changes, means a vertical split where we inherit the y values from the bounding box extent. The LitMax and BigMin values are now computed based on the x values in the same way as our first calculation, resulting in the LitMax point being (0111,0111) and BigMin point being (1000,0101) interleaved 00111111 = 63 and 01100010 = 98 dividing along the blue line. We still know that the last valid point was between 63 and 98, so we can start a regular scan from 98 and 107 which is our new bounding box. The new scan will result in new splits but at one point we'll return to the last reported value being larger than 107 and we'll start a regular scan from the BigMin calculated in our first split.

With our original bounding box we'll end up with 4 splits and 4 scans with a maximum of $(4-1) * 3$ false points reported.

There are another couple of observations to make: first the z value is a loss less representation of the x and y, so by storing z there is no need to store the x and y value. Another observation is that z is now just indexed as a one dimensional value; pre-pending it with any other one dimensional value would allow for even more specialized queries. Say you pre-pend it with type information than you can efficiently index any gas stations, any restaurants or any other type that you may discover at runtime without needing to ship the software with a predefined set of types.

4 CONCLUSION

To conclude the above discussion allows commercial off the shelf databases to dynamically and efficiently manage points-of-interest data without the need for specialized indexing techniques. It also supports on-device changes of data without the possibility of corruption.

5 COMPLETE SOURCE

Please download Raima's RDM Embedded technology for a running example of the problem described in this article, <http://www.raima.com/developer-tools/download-table/>

6 REFERENCES

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